

# The Space of Adversarial Strategies

USENIX'23

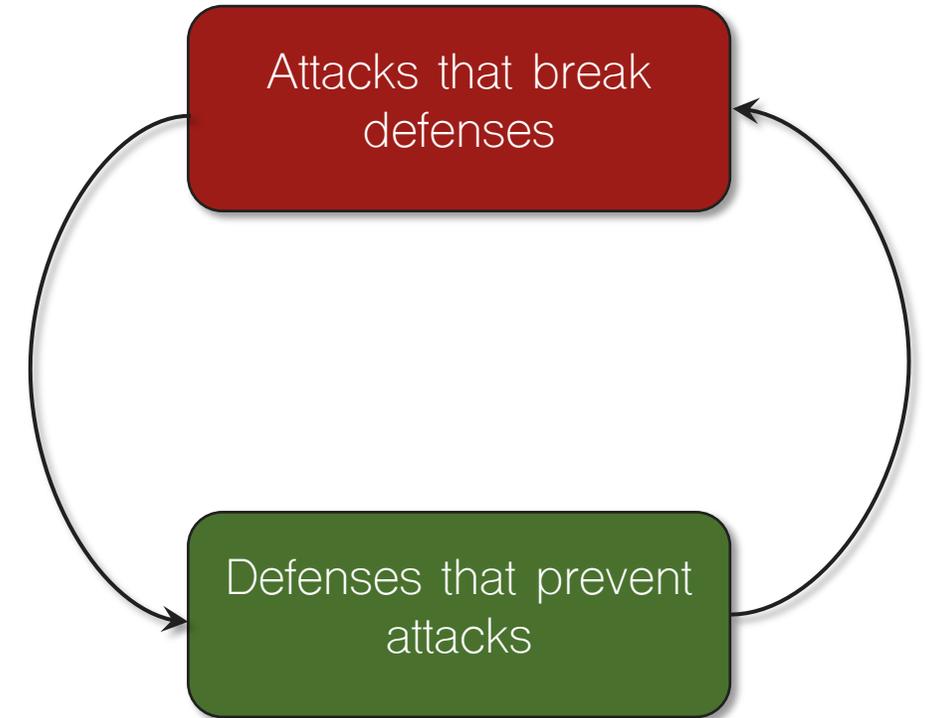
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Ryan Sheatsley\*, Blaine Hoak\*, Eric Pauley, Patrick McDaniel

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\*Equal Contribution. Thursday, August 10, 2023

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LaserAttack  
Adversarial Patch  
Projected Gradient Descent  
Frame Saliency Attack  
Geometric Decision Based Attack  
Malware Gradient Descent  
DeepFool  
RobustDPatch  
Over The Air Flickering Attack  
GRAPHITE  
High Confidence Low Uncertainty Attack  
Carlini and Wagner ASR  
Zeroth-Order Optimization  
Simple Black-box Adversarial Attack

Adversarial Texture  
NewtonFool  
Auto Conjugate Attack  
DPatch  
Auto Attack  
PixelAttack  
HopSkipJump  
Imperceptible ASR

LowProFool  
Brendel and Bethge Attack  
Targeted Universal Perturbation Attack  
Elastic Net Attack  
Fast Gradient Method  
Decision Tree Attack  
Shadow Attack

Basic Iterative Method  
Wasserstein Attack  
Carlini and Wagner  $l_0$   
Carlini and Wagner  $l_2$   
ThresholdAttack  
Carlini and Wagner  $l_\infty$   
Boundary Attack  
Universal Perturbation Attack  
Jacobian Saliency Map Approach  
Feature Adversaries

Square Attack  
Spatial Transforms Attack  
Sign-OPT  
Virtual Adversarial Method



• How can we systematically represent and evaluate attacks?



*Surfaces* compute the perturbation

*Travelers* apply perturbations and other techniques that update the input

**BIM**

$$\mathbf{X}_0^{adv} = \mathbf{X}$$

$$\mathbf{X}_{N+1}^{adv} = \text{Clip}_{\mathbf{X}, \epsilon} \left\{ \mathbf{X}_N^{adv} + \alpha \text{sign}(\nabla_{\mathbf{X}} J(\mathbf{X}_N^{adv}, y_{true})) \right\}$$

**FAB**

$$s \leftarrow \arg \min_{l \neq c} \frac{|f_l(x^{(i)}) - f_c(x^{(i)})|}{\|\nabla f_l(x^{(i)}) - \nabla f_c(x^{(i)})\|_q}$$

$$\delta^{(i)} \leftarrow \text{proj}_p(x^{(i)}, \pi_s, C)$$

$$\delta_{\text{orig}}^{(i)} \leftarrow \text{proj}_p(x_{\text{orig}}, \pi_s, C)$$

compute  $\alpha$  as in Equation (9)

$$x^{(i+1)} \leftarrow \text{proj}_C \left( (1 - \alpha) \left( x^{(i)} + \eta \delta^{(i)} \right) + \alpha \left( x_{\text{orig}} + \eta \delta_{\text{orig}}^{(i)} \right) \right)$$

**JSMA**

Compute forward derivative  $\nabla \mathbf{F}(\mathbf{X}^*)$

$$p_1, p_2 = \text{saliency\_map}(\nabla \mathbf{F}(\mathbf{X}^*), \Gamma, \mathbf{Y}^*)$$

Modify  $p_1$  and  $p_2$  in  $\mathbf{X}^*$  by  $\theta$

$$z^{(k+1)} \leftarrow P_S \left( x^{(k)} + \eta \nabla f(x^{(k)}) \right)$$

$$x^{(k+1)} \leftarrow P_S \left( x^{(k)} + \alpha (z^{(k+1)} - x^{(k)}) + (1 - \alpha) (x^{(k)} - x^{(k-1)}) \right)$$

**APGD**

$$\hat{l} \leftarrow \arg \min_{k \neq \hat{k}(x_0)} \frac{|f'_k|}{\|\mathbf{w}'_k\|_2}$$

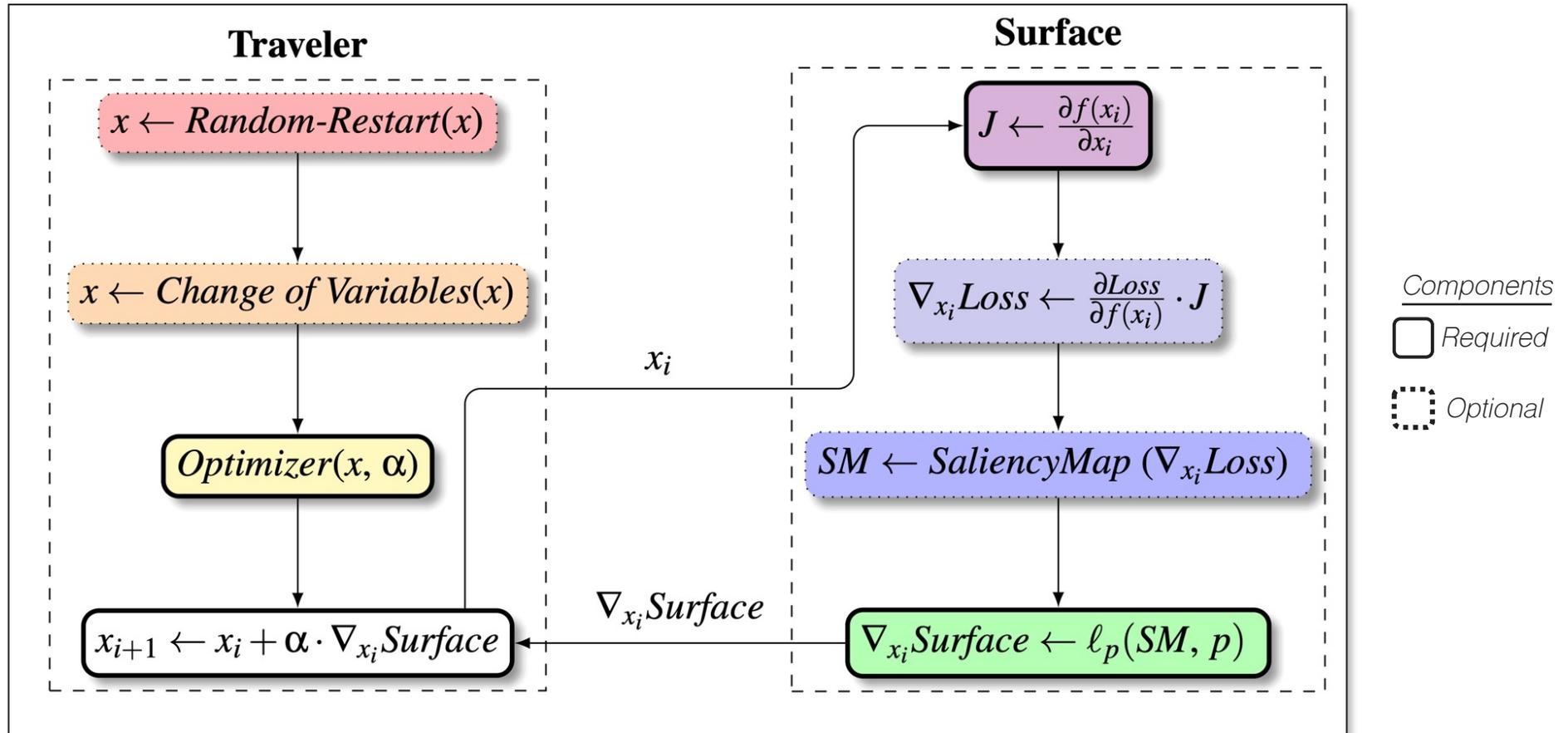
$$\mathbf{r}_i \leftarrow \frac{|f'_i|}{\|\mathbf{w}'_i\|_2} \mathbf{w}'_i$$

$$\mathbf{x}_{i+1} \leftarrow \mathbf{x}_i + \mathbf{r}_i$$

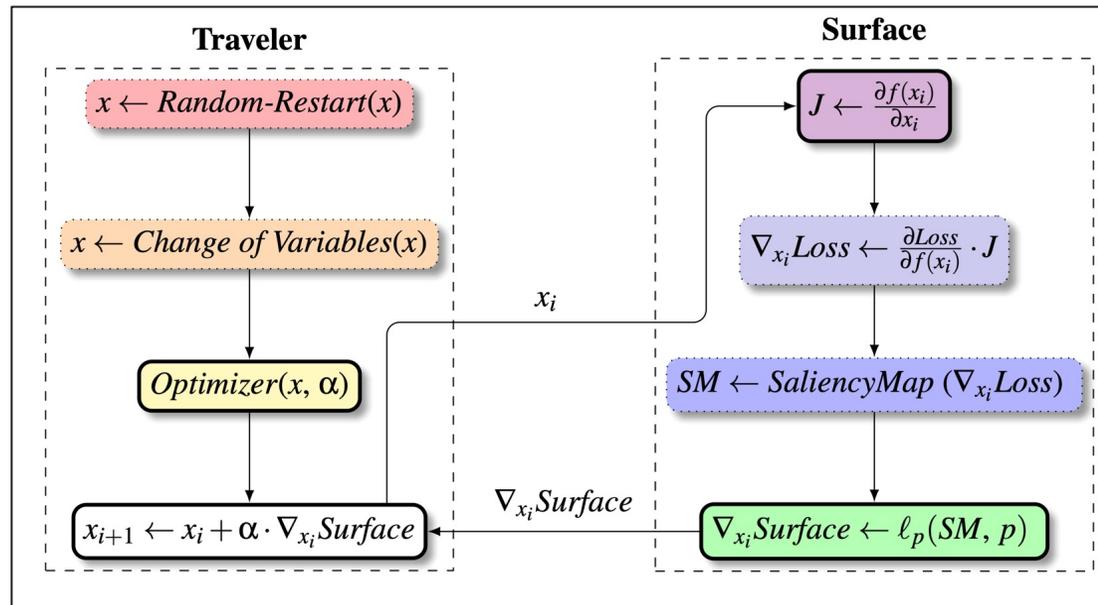
**DeepFool**

$$x^{t+1} = \Pi_{\mathbf{x}+S} \left( x^t + \alpha \text{sgn}(\nabla_x L(\theta, x, y)) \right)$$

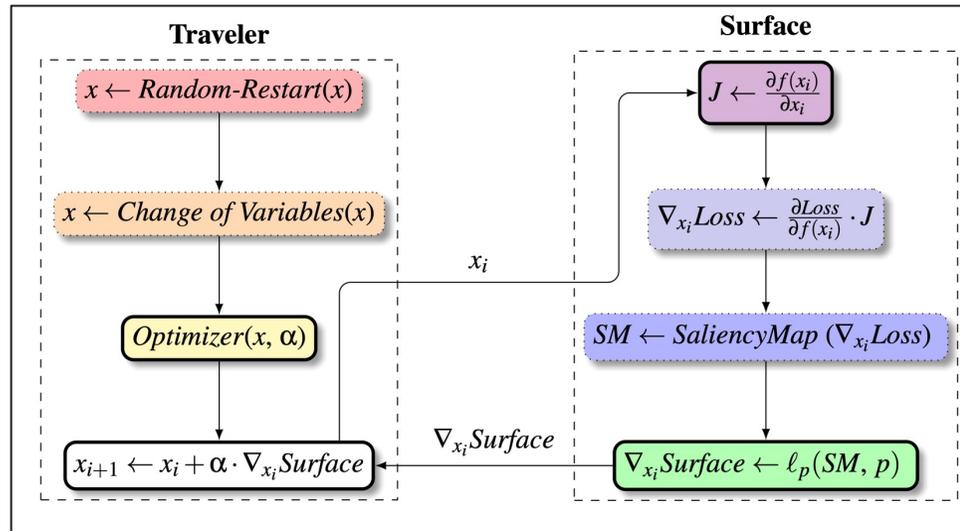
**PGD**



**Components of the traveler and surface. Arrows represent the progression of an an attack through components at each iteration.**



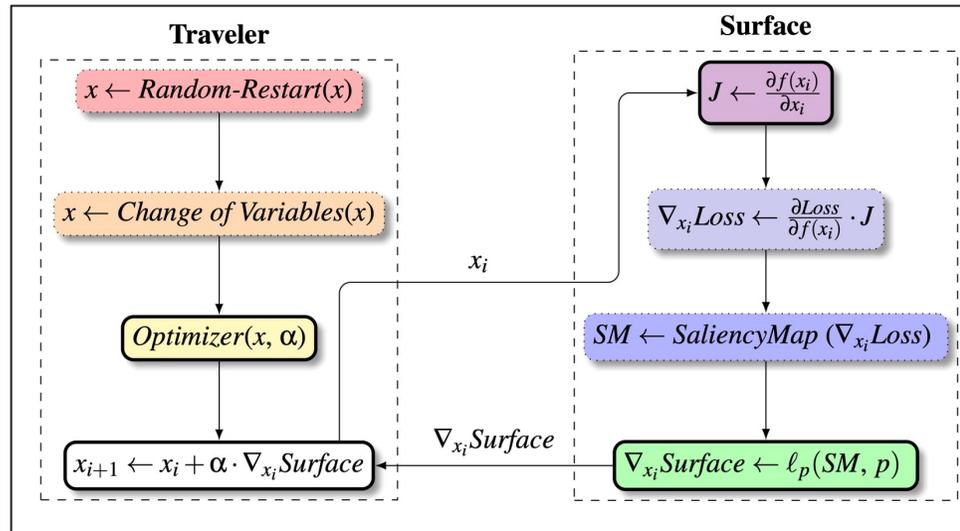
		Attack Algorithms															
		Surface Components							Traveler Components								
<i>Losses:</i>	Cross-Entropy								<i>Random-Restart:</i>	Enabled	Disabled						
	Carlini-Wagner Loss																
	Identity Loss																
	Difference of Logits Ratio Loss																
<i>Saliency Maps:</i>	$SM_J, SM_D, SM_I$								<i>Change of Variables:</i>	Enabled	Disabled						
	$\ell_p$ -norm $\ell_0, \ell_2, \ell_\infty$								<i>Optimizer:</i>	SGD	Adam	MBS	BWSGD				
	BIM	●	○	○	○	○	○	●	○	○	○	○	○	○			
	PGD	●	○	○	○	○	○	●	○	●	○	○	○	○			
	JSMA	○	○	●	○	●	○	○	○	○	○	○	○	○			
	DF	○	○	●	○	○	○	○	○	○	○	○	○	○			
	CW	○	●	○	○	○	○	○	○	○	○	○	○	○			
	APGD-CE	●	○	○	○	○	○	○	○	○	○	○	○	○			
	APGD-DLR	○	○	○	●	○	○	○	○	○	○	○	○	○			
	FAB	○	○	○	○	○	○	○	○	○	○	○	○	○			
		CE	CW	IL	DLR	$SM_J$	$SM_D$	$SM_I$	$\ell_0$	$\ell_2$	$\ell_\infty$	RR	CoV	SGD	Adam	MBS	BWSGD



Attack Algorithms																
Surface Components								Traveler Components								
Losses: Cross-Entropy Carlini-Wagner Loss Identity Loss Difference of Logits Ratio Loss								Random-Restart: Enabled, Disabled								
Saliency Maps: $SM_J, SM_D, SM_I$ $l_p$ -norm: $l_0, l_2, l_\infty$								Change of Variables: Enabled, Disabled Optimizer: SGD, Adam, MBS, BWSGD								
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JSM	○	○	○	○	○	○	○	○	○	○	○	○	○	○	○	
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PGD:  $\nabla \text{CE}(x, y)$

DeepFool:  $\nabla f_y(x)$

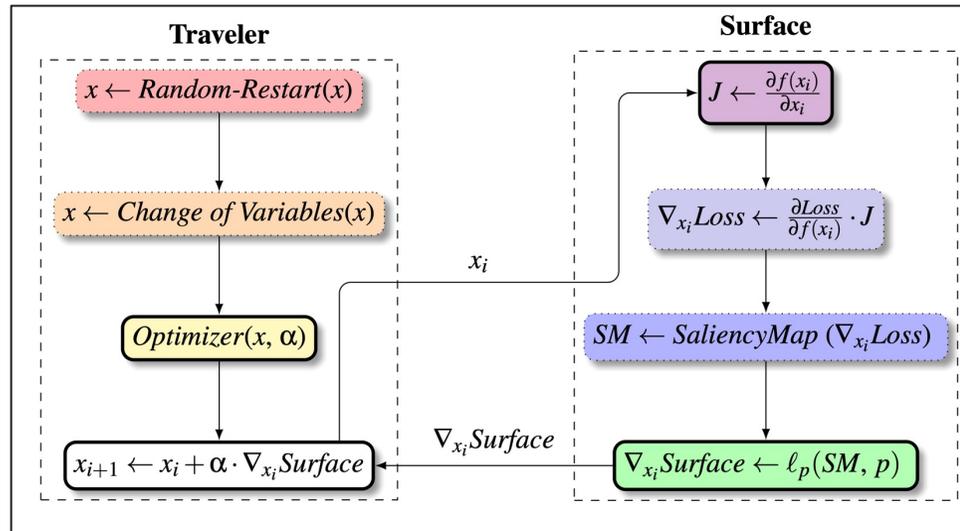


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Saliency Maps:				SM <sub>J</sub> , SM <sub>D</sub> , SM <sub>I</sub> ℓ <sub>p</sub> -norm ℓ <sub>0</sub> , ℓ <sub>2</sub> , ℓ <sub>∞</sub>				Change of Variables:				Enabled, Disabled				
								Optimizer:				SGD, Adam, MBS, BWSGD				
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PGD:  $\nabla \text{CE}(x, y)$

DeepFool:  $\frac{|f_y(x) - f_k(x)|}{\nabla f_y(x) - \nabla f_k(x)} (\nabla f_y(x) - \nabla f_k(x))$

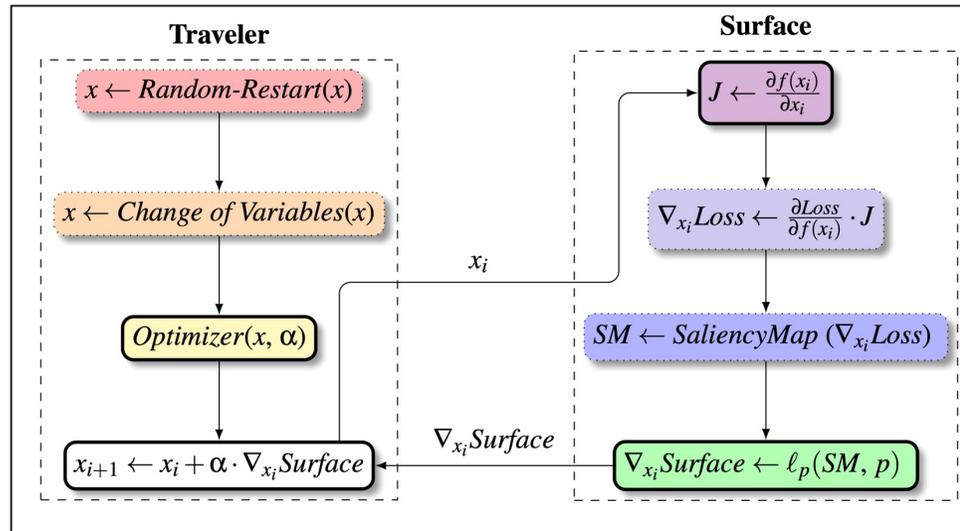




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PGD:  $\delta = \alpha \cdot \text{sgn}(\nabla \text{CE}(x, y)), x_0 = x + \mathcal{U}(-\epsilon, \epsilon)$

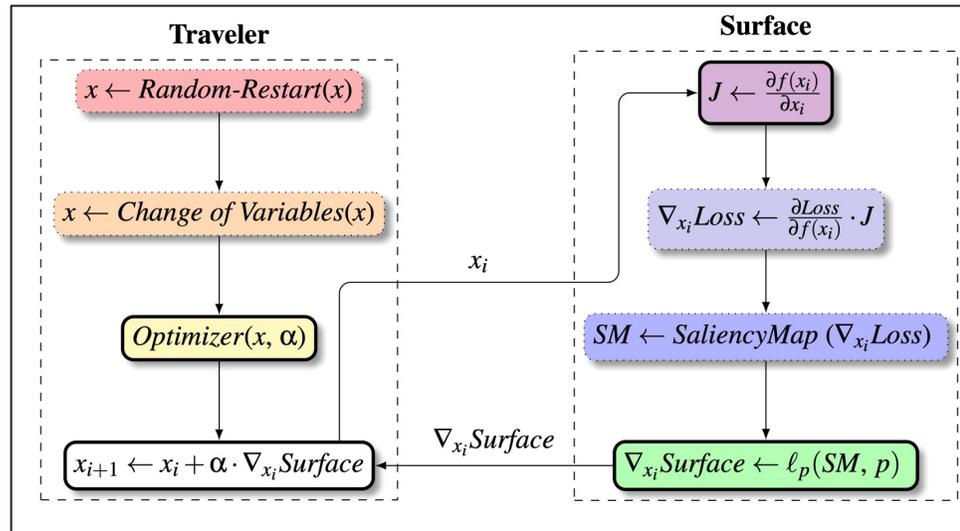
DeepFool:  $\delta = \frac{|f_y(x) - f_k(x)|}{\|\nabla f_y(x) - \nabla f_k(x)\|_2} \cdot (\nabla f_y(x) - \nabla f_k(x)), x_0 = x$



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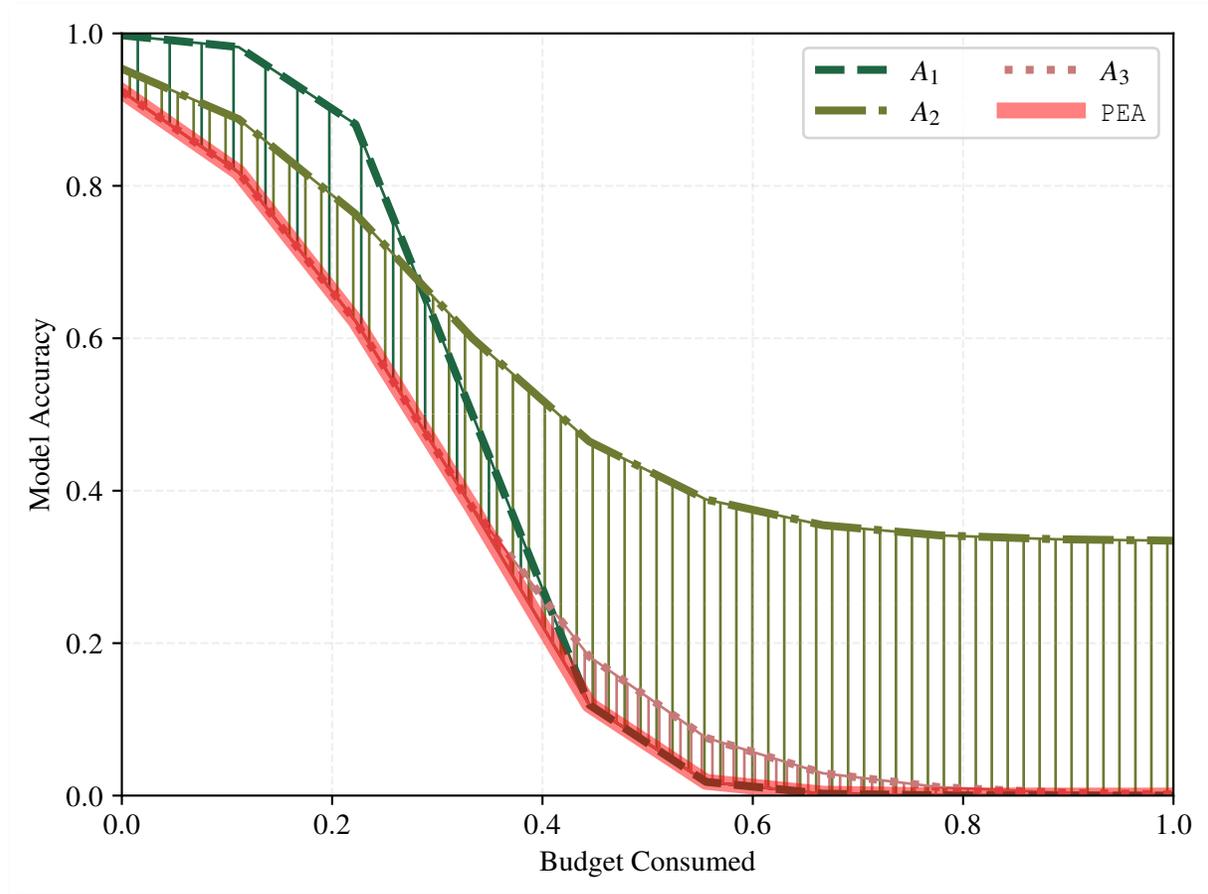


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	CE	CWL	IL	DLR	SM <sub>J</sub>	SM <sub>D</sub>	SM <sub>I</sub>	ℓ <sub>0</sub>	ℓ <sub>2</sub>	ℓ <sub>∞</sub>	RR	CoV	SGD	Adam	MBS	BWSGD

Our **extensible** decomposition of **mutually compatible and independent** components allows us to build a vast attack space containing 576 attacks.



## *The Pareto Ensemble Attack*





# Evaluation

- Questions
  - When and why are attacks performant?
- Setup
  - Adversary has access to model parameters
  - CIC-MalMem2022, **Malware Detection**, 58k total (k-Fold), 4 classes
  - CIFAR-10, **Object Classification**, 50k train, 10k test, 10 classes
  - Fashion-MNIST, **Clothing Classification**, 60k train, 10k test, 10 classes
  - MNIST, **Digit Recognition**, 60k train, 10k test, 10 classes
  - NSL-KDD, **Network Intrusion Detection**, 125k train, 22k test, 5 classes
  - Phishing Websites, **Phishing Detection**, 10k total (k-Fold), 2 classes
  - UNSW-NB15, **Network Intrusion Detection**, 101k train, 53k test, 10 classes



# Hypothesis Testing Illuminates Effective Strategies

	Component H <sub>1</sub>		Component H <sub>2</sub>		Condition	p-value	Effect Size
1.	SGD	is better than	BWSGD	when	Dataset = MNIST	$<2.2 \times 10^{-308}$	99 %
2.	Adam	is better than	BWSGD	when	Dataset = MNIST	$<2.2 \times 10^{-308}$	99 %
		⋮					
84.	Identity Loss	is better than	Difference of Logits Ratio Loss	when	Dataset = NSL-KDD	$<2.2 \times 10^{-308}$	93 %
85.	SGD	is better than	BWSGD	when	SaliencyMap = Jacobian Saliency Map	$<2.2 \times 10^{-308}$	92 %
		⋮					
393.	DeepFool Saliency Map	is better than	Jacobian Saliency Map	when	Dataset = FMNIST	$<5 \times 10^{-6}$	66 %
394.	Cross-Entropy	is better than	Carlini-Wagner Loss	when	Change of Variables = Disabled	$<5 \times 10^{-6}$	61 %
		⋮					
1689.	$\ell_0$	is better than	$\ell_2$	when	Threat Model = $\ell_2 + 1.0$	$9.8 \times 10^{-1}$	50 %
1690.	Identity Saliency Map	is better than	DeepFool Saliency Map	when	Threat Model = $\ell_\infty + 0.4$	1.0	49 %



## *Hypothesis Testing Illuminates Effective Strategies*

- Change of Variables → 100% disabled, 0% enabled
- Optimizers → 50% Adam, 33% SGD, 16% MBS, 1% BWSGD
- Random Restart → 61% enabled, 39% disabled
- Saliency Maps → 70% no Saliency Map, 30% either DeepFool or JSMA Saliency Map
- Loss → 47% Identity Loss, 34% Cross Entropy, 18% Carlini Wagner Loss, 1% DLR Loss



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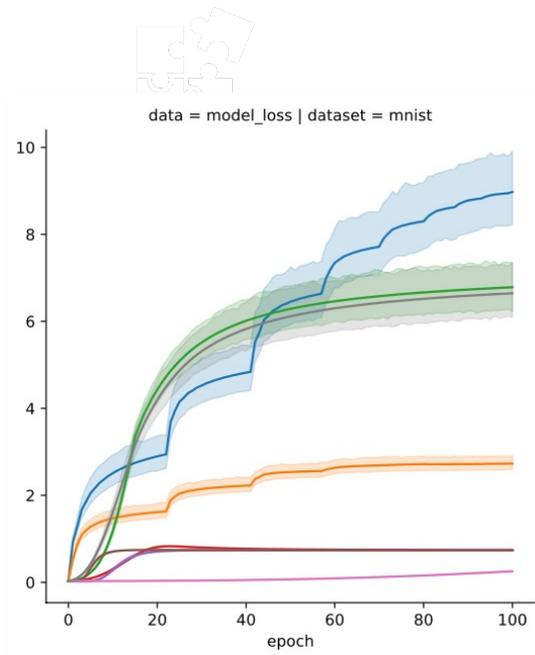


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# GitHub Repo: <https://github.com/sheatsley/attacks>



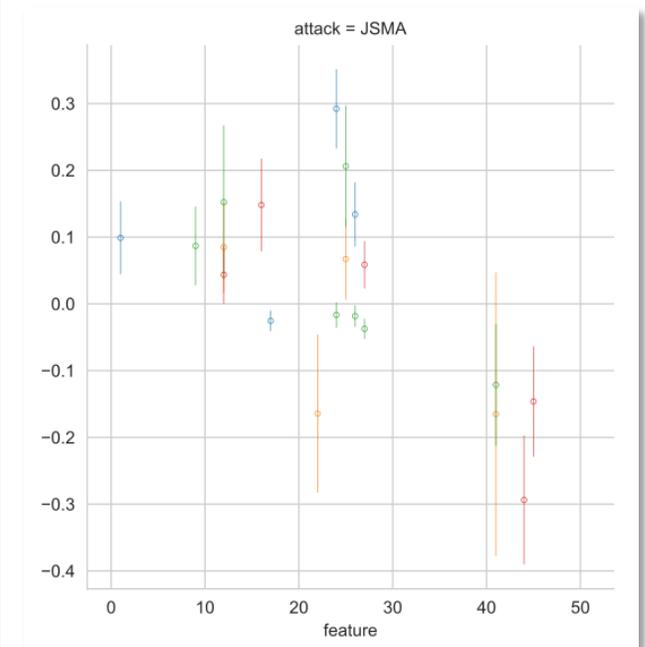
sheatsley add perturbation visualization figure for mnist c23e797 19 hours ago 401 commits

- aml adapt version computation to load static version file for non-dev ins... 2 days ago
- examples add perturbation visualization figure for mnist 19 hours ago
- .gitmodules add overleaf ref 7 months ago
- Dockerfile refactor dockerfile to build off of models 20 hours ago
- LICENSE add license 6 months ago
- README.md typofixes 2 days ago
- setup.py always generate version file 2 days ago
- tests.py reset seeds after fit to ensure results consistency when loading pret... yesterday

## Adversarial Machine Learning

*Adversarial Machine Learning* (`aml`) is a repo for measuring the robustness of deep learning models against white-box evasion attacks. Designed for academics, it is principally designed for use in fundamental research to understand *adversarial examples*, *inputs designed to cause models to make a mistake*. At its core, `aml` is based on a series of techniques used in eight popular attacks:

1. [APGD-CE](#) (Auto-PGD with CE loss)
2. [APGD-DLR](#) (Auto-PGD with DLR loss)
3. [BIM](#) (Basic Iterative Method)
4. [CW-L2](#) (Carlini-Wagner with L2 norm)
5. [DF](#) (DeepFool)
6. [FAB](#) (Fast Adaptive Boundary)
7. [JSMA](#) (Jacobian Saliency Map Approach)
8. [PGD](#) (Projected Gradient Descent)





# Thank you

 <https://hoak.me>

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 [@blaine\\_hoak](https://twitter.com/blaine_hoak)

 [blainehoak](https://github.com/blainehoak)